

Using Number Talks to Build and Support Questioning and Discourse

December 2017

Learning Targets

- I can describe how number sense leads to algebraic thinking.
- I can describe how using number talks can help teachers make student thinking visible.
- I can describe how using number talks can help to hone teacher questioning skills.

How many different ways can you
show 22×28 ?

Pause the video while you explore the different ways to show
 22×28

Some strategies you may have come
up with...

Share with a colleague all the strategies you came up with.

*How are the strategies similar to or different from the
strategies that follow?*

Strategy 1
22x28

Traditional Algorithm

$$22 \times 28$$

$$\begin{array}{r} \overset{10}{22} \\ \times 28 \\ \hline 176 \\ 440 \\ \hline 616 \end{array}$$

Strategy 2

22x28

Break a Factor Into
Two or More Addends

$$\begin{array}{r} 22 \times 28 \\ 28(20+2) \\ 560+56 \\ \hline 616 \end{array}$$

Area Model

	20	2
28	560	56

$$\begin{array}{r} 560+56 \\ \hline 616 \end{array}$$

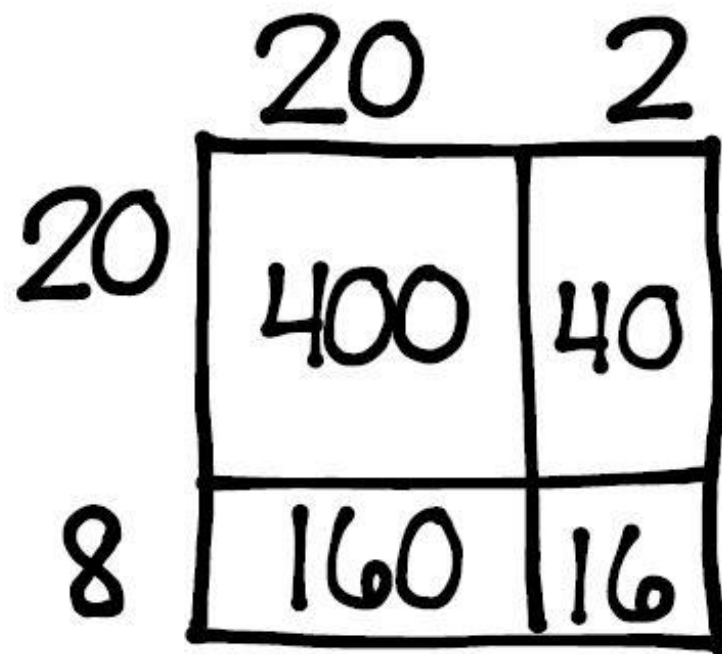
Strategy 2 cont.

22x28

Break Both Factors Into
Two or More Addends

$$\begin{aligned} &22 \times 28 \\ &(20+2)(20+8) \\ &400+160+40+16 \\ &616 \end{aligned}$$

Area Model



Strategy 3

22x28

Break a Factor Into Smaller Factors

$$22 \times 28$$

$$22 = (2)(11)$$

$$28 = (2)(2)(7)$$

$$(11)(7) = 77$$

$$(77)(2) = 154$$

$$(154)(2) = 308$$

$$(308)(2) = 616$$

Strategy 4

22x28

Round a Factor and Adjust

$$22 \times 28$$

Round 28 to 30

$$(22)(30) = 660$$

$$660 - 2(22)$$

$$660 - 44$$

$$616$$

Strategy 5

22x28

Halving and Doubling

$$22 \times 28$$

$$44 \times 14$$

$$88 \times 7$$

$$616$$

Using Teacher Questioning

- Choose one of the strategies.
- What questions might you ask a student to better understand the mathematical decisions and thinking processes they utilized when solving the problem using that particular strategy?
- Pause for personal reflections and/or discussions

Possible questions for each strategy

- Traditional Algorithm:
 - What is the actual value of this digit?
 - What does it mean to carry?
 - Why do you write that digit above the tens column?
 - Why is it that when you multiply 2 by 8 and carry the 1, do you add it to the product of 8×2 ?
 - How could you represent your thinking with a picture?
 - Why do you move over one place when you are doing the second multiplication?
- Breaking Factors into Addends
 - How did changing 22 into 20 plus 2 (or 28 into 20 plus 8) help you solve the problem?
 - Why didn't breaking up the 22 and/or the 28 change the value of the answer?
 - How did you decide to break up the factor(s) that way?

Possible questions for each strategy

- Breaking Factors into Smaller Factors
 - How did you decide which number to factor?
 - How did you decide which factors to use?
 - How did factoring 22 (or 28) make the problem easier?
 - Why does this strategy work?
- Rounding and Adjusting
 - How did rounding the factor to 20 (or 30) make this problem easier?
 - How did you know what to subtract (or add)?
 - How did you decide which factor to round?
- Halving and Doubling
 - How did you decide which number to double and which number to halve?
 - Why did that make it an easier problem to think about?

Shifting Gears – Arithmetic to Algebra

What are the different properties of real numbers that allow students to utilize the various strategies for multiplying 22×28 ?

Pause for personal reflections and/or discussions.

What are the misconceptions that students have when multiplying polynomials?

Pause the video to generate a list of misconceptions you have seen students bring to the table when multiplying polynomials.

How many different ways can you
show $(x+3)(x+5)$?

Pause the video to generate as many ways to show $(x+3)(x+5)$.

Pause for personal reflection and/or share with a colleague.

One way to visually show $(x+3)(x+5)$ is...

Area Model

	x	3
x	x^2	$3x$
5	$5x$	15

$x^2 + \underline{3x} + \underline{5x} + 15$
 $x^2 + 8x + 15$

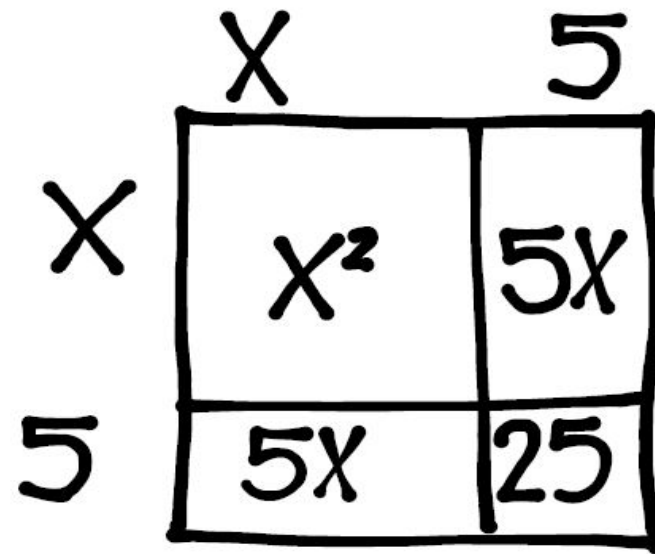
How many different ways can you show $(x+5)^2$?

Pause the video to generate as many ways to show $(x+5)^2$.

Pause for personal reflection and/or share with a colleague.

One way to visually show $(x+5)^2$ is...

Area Model



$$x^2 + \underline{5x} + \underline{5x} + 25$$

$$x^2 + 10x + 25$$

Connections and Reflections

Pause the video to discuss and reflect on the following...

- How is modeling 22×28 similar to and different from modeling $(x+5)^2$?
- How does visualizing 22×28 build a strong foundation for visualizing and modeling $(x+5)^2$?

Jeremy's Video

Jeremy's Video- Student Strategies

$$22 \cdot 28$$

	20	2
20	400	40
8	160	16

$400 + 40 = 440$
 $160 + 16 = 176$
 Francisco 616

$$22 \cdot 28$$

$$\begin{array}{r} 22 \\ \times 28 \\ \hline 176 \\ 440 \\ \hline 616 \end{array}$$

Bryce 616

$$22 \cdot 28$$

$$22(20+8)$$

$$22 \cdot 20 = 440$$

$$22 \cdot 8 = 176$$

Paola 616

$$22 \cdot 28$$

$$\begin{array}{r} 28 \\ \times 22 \\ \hline 116 \\ 160 \\ \hline 400 \\ \hline 616 \end{array}$$

Stacie 616

$$22 \cdot 28$$

$$22 \rightarrow 20$$

$$28 \rightarrow 30$$

$$20 \cdot 30 = 600$$

$$8 \cdot 2 = 16$$

Zaney 616

$$22 \cdot 28$$

$$(20+2) \cdot 28$$

$$28 \cdot 20 = 560$$

$$28 \cdot 2 = 56$$

Zaney 616

$$22 \cdot 28$$

$$\begin{array}{r} 22 \\ \times 28 \\ \hline 176 \\ 440 \\ \hline 616 \end{array}$$

Sergio

$$22 \cdot 28$$

$$\begin{array}{r} 28 \\ \times 22 \\ \hline 116 \\ 560 \\ \hline 616 \end{array}$$

Sergio

$$22 \cdot 28$$

$$22(30-2)$$

$$22 \cdot 30 = 660$$

$$22 \cdot -2 = -44$$

Zaney 616

Video Reflection

Pause the video to discuss and reflect on the following...

- How did the number talk protocol explicitly support making student thinking visible and why is it important?
- How did questioning play a role in revealing student thinking?

Video Reflection con't

Pause the video to discuss and reflect on the following...

- What does it do for student learning and understanding when we are able to support them in visualizing the mathematics they are engaged in?
- How do the questions we ask make the mathematics visible to all students?

Self-Reflection & Action Planning

On your own, reflect on the following...

- What professional learning are you walking away with today?
- What will you commit to between now and next week to implement what you have learned?

Additional Resources

- <https://www.youcubed.org/resources/stanford-onlines-learn-math-teachers-parents-number-talks/>