## Welcome!

This webinar was pre-recorded on Wednesday, March 23, 2016. There were no FAQs generated during the live presentation.

Please submit any questions or comments to mc2@nmsu.edu.

# Addition \& Subtraction within 100 

Extending Conceptual Place Value

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## Learning Targets

- Understand the research-based instructional progression that supports students as they develop strategies based on place value
- Understand how the fluency progression outlined in the CCSSM develops for students
- Explore instructional alternatives to column addition \& subtraction (the algorithm)


## Place Value: Phases of Instruction

- Phase I: Developing Foundational Knowledge
- Phase 2: Consolidating Early Strategies
- Phase 3: Refining Strategies and Extending Tasks


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# Instructional Progression for <br> Number \& Operations in Base Ten 



Phase 2: Develop Mental Computation open tasks, students grapple with solutions tasks presented with base ten models (not manipulated) tasks posed as number talks and in story contexts

Phase 3: Refine and Extend Mental Strategies
formalize notation, bigger numbers, strategic tasks

## CCSSM: <br> Number \& Operations in Base Ten

2.NBT. 5

Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.
3.NBT. 2

Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
4.NBT. 4

Fluently add and subtract multi-digit whole numbers using the standard algorithm.

## CCSSM: <br> Number \& Operations in Base Ten

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## Think of a couple mental strategies for solving

## $47+28$

(try not to mentally stack the numbers and use the algorithm)

## 2nd Grade Student: 47+28



## Assessment: Expression Cards

- Ask student to read and solve the task
- Ask student to explain how they got the answer
- If student uses the standard algorithm, ask if there is another way they could solve it
- This assessment is used to determine facility with strategies based on place value the student has developed for solving 2 -digit addition \& subtraction tasks


## 2nd Grade Student



$$
52+24 \cdot 35-21 \cdot 47+28 \cdot 73-38
$$

## Analyzing the Assessment:

What prior knowledge is the student using:
Starts with adding the tens, then the ones
When adding 7+8, makes a 10 out of the two 5 s
Areas to work on:
Develop fluency with addition and subtraction within 20
Subtraction tasks: make sense using models, use notation to show successful strategies using numbers


73-38


## Assessment: Expression Cards

If a student is...

- unable to solve some or all of the tasks
- only able to solve tasks using the algorithm ...use the dot strips assessment to check whether they have strategies for adding tens \& ones with materials


## 2nd Grade Student $47+28$, task with numbers



## 2nd Grade Student 47+14, dot strips



## Informal Notation:

 numbers are used to show strategies used to solve dot strips tasks$$
\begin{aligned}
& 47+14 \\
& 4071024 \\
& 40+10 \rightarrow 50+7 \rightarrow 57+4 \rightarrow 61
\end{aligned}
$$

## Field Trip Addition



- Students select 2 bus cards
- Record the number of kids on each bus on their record sheet
- Use the cards to determine the total number of kids


## 2nd Grade: Field Trip Addition 37 + 18



## Split Strategy:

## Working with the Tens, then the Ones

## $37+18$

## Informal Notation:

- notation matches student thinking
- use arrows, not equal sign, when showing a running record of the solution
- when students split numbers into parts, use drop-down notation to indicate the parts
- notation can be modeled in number talks


## Number Talks

- a 10-15 minute routine, 3 or more times a week
- students solve problems using mental strategies
- students develop communication skills as they explain their reasoning
- teacher records solutions in a way that reflects students' strategies
- for more information, see the $M C^{2}$ website


## 2nd Grade: 32 - I7



Number Rack App: Math Learning Center website and the App Store for iOS devices

## Number Talks: Other Models



Number Frames App:

- Math Learning Center website
- The App Store for iOS devices


Unifix cubes / Snap cubes: 36-19

## New Mexico Travel: Interstate 25

Get on at Exit 75 Williamsburg.
Travel south to Radium Springs: the trip is 56 miles.
What is the exit number for Radium Springs?


## Instructional Progression for Number \& Operations in Base Ten

## Phase I:Foundation: <br> Structuring Numbers to 20 (\& into higher decades) <br> Conceptual Place Value

Phase 2: Develop Mental Computation open tasks, students grapple with solutions tasks presented with base ten models (not manipulated) tasks posed as number talks and in story contexts

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## Thank you!

## This webinar recording and handouts are available at the $\mathrm{MC}^{2}$ website.

Please submit any questions or comments to mc2@nmsu.edu.

Thank you for your input!
$M C^{2}$ is always striving to improve the learning experience.

